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Bandwidth Efficient Synchronous Tuning (BEST) for Improved Very-Low-Frequency and Low-Frequency (VLF/LF) Communications

Richard W. Middlestead Telecommunication Science Associates, Inc. San Diego, CA 92103

Peder M. Hansen Naval Ocean Systems Center San Diego, CA 92152

Abstract

Synchronously tuning a transmit antenna to the instantaneous tones of a frequency modulated waveform can result in enormous improvements in radiated power efficiency and data detection. The best performance is obtained when the modulation waveform tones are phase continuous and when the maximum tone separation is much smaller than the operating frequency. Both of these conditions are satisfied by most systems. The advantages in using Bandwidth Efficient Synchronous Tuning (BEST) are realized by a significant reduction in the loss and distortion affects usually associated with fixed tuned antennas. This paper characterizes the performance of

continuous-phase frequency-shift-keying (FSK) and minimum-shift-keying (MSK) modulated waveforms with synchronous the transmit tuning of antenna. Analysis and computer simulation results support the conclusion that there is less than 0.5 dB degradation in the bit-error-probability performance for instantaneous antenna bandwidths(B) several orders than the modulation magnitude less bandwidth (1/T). Also, the radiated power can be increased by as much as 7 dB, for time-bandwidth (BT) products as low as 0.3, through the elimination of the flat loss and amplitude distortion usually associated with fixed tuned antennas.

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Abstract

This paper characterizes the performance continuous-phase frequency-shift-keying minimum-shift-keying (FSK) and modulated waveforms with synchronous tuning of the transmit antenna. Analysis and computer simulation results support the conclusion that there is less than 0.5 dB degradation in the bit-error-probability performance for instantaneous antenna bandwidths(B) several orders of magnitude less than the modulation bandwidth (1/T). Also, the radiated power can be increased by as much as 7 dB.

I. Introduction

Bandwidth efficient synchronous tuning (BEST) is an antenna tuning technique, applied at the transmit site, for reducing the loss and distortion of a signal radiated by a narrow bandwidth antenna. Synchronous tuning means that the resonant frequency of the transmit antenna is tuned to the instantaneous frequency of the modulated signal waveform. The analysis undertaken in this paper focuses on ideally modulated discrete frequency waveforms like M-ary Frequency-Shift-Keying (FSK) and Minimum-An example of the Shift-Keying (MSK). antenna tuning in the frequency domain is shown in Figure 1 for an ideally modulated binary-FSK waveform having a unity modulation index. In this situation, the modulation tone separation is $\Delta f \ = \ R_b$, where R_b is the modulation data rate.

The antenna switches to the lower modulation tone position (the dashed curve) as determined by the tuning control voltage. For binary-FSK and MSK, the minimum duration that the antenna is tuned to any tone is $T_b = R_b^{-1}$ seconds. More generally, for M-ary FSK this duration is the symbol duration $T = T_b$ log2(M). The time-bandwidth product BT (or BTh) is a convenient parameter with which to characterize various performance measures.

The practical advantages associated with synchronously tuning a high-Q transmit antenna have been known and explored for many years (refs. 1 and 2). These efforts have concentrated principally on very-low-frequency (VLF) applications for U.S. Navy submarine communications and in particular have focused on various techniques for tuning the large, high-power antennas. The technical problems associated with the switching of high power and physically large tuning elements are still being investigated. These continuing efforts are necessary to keep pace with the development of the high power solid-state amplifier technology.

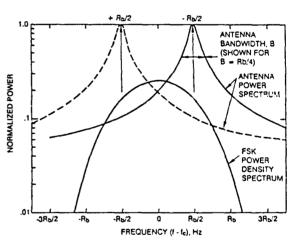


Figure 1. Relationship Between Binary-FSK Signal Spectrum and Synchronously Tuned Antenna Frequency Response

II. Background In this section, the various system losses are characterized for an MSK modulated *I waveform with data rate 1/Tb using a conventional fixed tuned transmit antenna.

The resulting losses will serve as a ad



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background to dramatize the potential performance advantages of synchronous antenna tuning developed in the following sections. Because the antenna is tuned to a fixed frequency, it can be conveniently modeled by the equivalent baseband transfer function expressed as

$$H(\mu) = \frac{K}{1 + j \left(\frac{2\mu}{R}\right)}$$
 (1)

where μ = f - f_C is the equivalent lowpass frequency, f_C is the center frequency, which is the same as the modulation carrier frequency, and B is the two-sided 3 dB bandwidth in Hz. The various sources of performance loss are the fixed loss, the receiver detection loss resulting from intersymbol interference (ISI), and the power back-off loss. The losses are shown in Fig. 2 for the fixed tuned antenna.

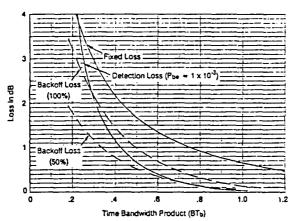


Figure 2. Various Power Losses Associated with an MSK Modulated Waveform through a Fixed Tuned Transmit Antenna

III. Synchronous Antenna Tuning

From the results of the preceding section, it is clear that enormous communication system performance penalties can result from fixed tuned narrowband transmit antennas operating with sufficiently low BTb products. In this section, the various sources of degradation are revisited in the context of synchronous antenna tuning. The analysis applies to a modulation waveform consisting of an arbitrary number of discrete tones as described by

$$e_i(t) = A \cos(\omega_c t + \overline{\omega}_i t + \theta_i)$$
 (2)

where A establishes an arbitrary signal amplitude, $\omega_{\rm C}$ represents the average carrier angular frequency of the tone set

$$\{\omega_i = \omega_C + \overline{\omega}_i\}, \overline{\omega}_i$$
 is the instantaneous

baseband angular frequency of the modulation, and θ_i represents a phase angle, which has a data dependent component for MSK. For the various forms of modulation considered, the transition between the frequencies is assumed to be instantaneous, thus the synchronous antenna tuning is not considered for a variety of so called tamed frequency modulated waveforms.

The antenna circuit is modeled, as in the preceding section, as a single-time-constant series tuned RLC circuit. The synchronous tuning is achieved by appropriately changing the circuit inductance L_i . The synchronous antenna tuning results in a linear time-varying circuit which is, at best, difficult to model in terms of baseband functions. In the frequency domain, the antenna is described by the dynamic system function

$$H_{i}(\omega;t) = \frac{2}{R} \frac{j\omega\alpha_{i}}{(j\omega+\alpha_{i})^{2}+\beta_{i}^{2}}$$
(3)

For this analysis the solution is formulated in terms of state variables, which are particularly appropriate because the coefficients are constant over discrete time intervals. The differential equation of the antenna circuit model is given by

$$\dot{q}(t) + 2\alpha_{i}\dot{q}(t) + \nu_{i}^{2}q(t) = \frac{2\alpha_{i}}{R} e_{i}(t)$$

The state variables are defined in terms of the circuit charge, q(t), as

$$X_1(t) = q(t)$$
 and $X_2(t) = q(t)$.

To evaluate the radiated signal strength from the antenna, it is necessary to evaluate the antenna current given by $i(t) = X_2(t)$.

The result is

$$i(\tau) = C X(\tau)$$
 (5)

where $C = (0\ 1)$ is the output coupling vector and $X(\tau)$ is the system state vector given by

$$X(\tau) = \phi(\tau, t_{i-1})X(t_{i-1}) + \int_{t_{i-1}}^{\tau} \phi(\tau, \varsigma)B(\varsigma)e_{i}(\varsigma)d\varsigma$$
$$\tau \ge t_{i-1}$$
 (6)

In equation 6, $\phi(\tau,t)$ is the state transition matrix and

$$B(\tau)=B_i=(0 \frac{2\alpha_i}{R})^T$$

is the input coupling vector. Equation 6 relates the change in the system state vector with time relative to the conditions at time $t=t_{i-1}$. In this regard, the first term represents the initial condition response and the second represents the forced response which is characterized by the superposition integral. To evaluate the response of the synchronously tuned antenna, advantage is taken of the time invariance of the coefficients over discrete intervals $[t_{i-1}, t_{i}] = [iT - T, iT]$, in which case equation 6 involves the simplified convolutional integral and is formulated as

$$i_i(\tau) = CX_i(\tau) \tag{7}$$

$$X_{i}(\tau) = \phi_{i} \left(t_{i-1}^{-\tau} - \tau\right) X_{i}(t_{i-1}) +$$

$$\int_{t_{i-1}}^{\tau} \phi_{i}(\tau - \zeta) B_{i} e_{i}(\zeta) d\zeta$$
(8)

with $t_{i-1} \le \tau \le t_i$. In the remainder of this section, the characteristics of an isolated frequency transition are developed, followed by a general situation involving random contiguous frequency transitions in the modulation waveform.

a. <u>Isolated Frequency Transition</u> In examining the transient results of an isolated frequency transition in the

modulation waveform, considerable insight is obtained regarding the impact of various signal and antenna parameters, such as the data rate, modulation index, carrier phase continuity, operating frequency, and the antenna instantaneous bandwidth. For convenience, the isolated frequency transition is taken to occur at $t_{i-1} = t_0 = 0$. The details are too involved for this paper, however, the resulting signal at a distant receiver can be expressed as

$$e_{r}(t) = \sqrt{2P_{r}} \cos(\omega_{1}t + \phi_{1})$$

$$0 \le t \le 7$$

$$+ \sqrt{2P_{r}} M_{1}e^{-\pi Bt} \sin(\omega t_{1} + \phi_{1})$$

where P_r is an arbitrary received power level and the distortion parameters $\,M_1$ and $\,\Phi_1$ are given by

$$M_{1} = \left\{ \left[2 \sin(\phi_{0} + \phi_{\Delta}/2) \sin(\phi_{\Delta}/2) \right]^{2} + \left[2 \left[\cos(\phi_{0} + \phi_{\Delta}/2) - \frac{BT}{2} \left(\frac{R_{s}}{f_{c}} \right) \sin(\phi_{0} + \phi_{\Delta}/2) \right] \sin(\phi_{\Delta}/2) + \left(\frac{\Delta f_{1}}{f_{c}} \right) \sin(\phi_{0}) \right]^{2} \right\}^{1/2}$$

$$(10)$$

In equation 10 ϕ_0 is the phase at $t_0=0$ of the forcing function applied prior to $t_0=0$ and the angle $\phi_{\Lambda}=\phi_1-\phi_0$ represents the phase difference between the forcing functions at the instant of the transition. Continuous phase modulation waveforms require that $\phi_{\Lambda}=0$. Af $_1=f_1-f_0$ is the change in the tuning frequency in Hz. Using B instead of B_i and f_c instead of f_i are convenient substitutions which do not materially affect the results as long as the instantaneous carrier are much greater than either B_i or Δf_i .

The impact of the various parameters on the received signal is examined in terms of the normalized received energy-per-symbol which is given by

$$\frac{E_s}{E_s'} = \frac{1}{E_s'} \int_0^T e_r^2(t) dt$$
 (12)

= 1 -
$$\frac{2M_1}{\pi BT}$$
 (1 - $e^{-\pi BT}$) $\sin(\phi_0 + \phi_\Delta - \phi_1)$ (13)

where $E_{S}^{'}$ is the received energy-per-symbol without any distortion.

In addition to having CPM, it is desirable to operate under conditions for which $\Delta f_1/f_{\rm C}$ and BT result in a low symbol energy loss. To quantify the affect of these various parameters for CPM, the worst case loss is examined, which is seen from equation 13 to occur when $\phi_{\rm O}=90^{\circ}$. Thus, evaluating equation 13 for $\phi_{\rm A}=0^{\circ}$ and $\phi_{\rm O}=90^{\circ}$ results in

$$\frac{E_{S}}{E_{S}'} \begin{vmatrix} = 1 - 2 \frac{(\Delta f_{1}/f_{c})}{\pi BT} & (1 - e^{-\pi BT}) \\ \phi_{\Delta} = 0 & \end{cases}$$
 (14)

Equation 14 is plotted in Fig. 3 as a function of BT for various conditions of the normalized parameters $\Delta f_1/f_c$.

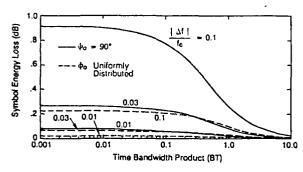


Figure 3. Maximum Symbol Energy Loss for Isolated Transition with CPM (ϕ_{Λ} = 0, ϕ_{O} = 90° and $\Delta f_{1} > 0$) and Continuous Phase Binary-FSK Modulation (ϕ_{Λ} = 0, ϕ_{O} uniformly distributed)

b. Multiple Frequency Transitions

The transient characteristics of the synchronously tuned antenna are now examined for the frequency modulated waveform consisting of multiple frequency transitions at discrete times $t=t_1=iT,\ i=0,1,2,\ldots$. The details in characterizing the expression for the signal at a distant receiver are too involved to present in this paper. However, using the same initial conditions as for the isolated frequency transition, the received

signal during the N-th symbol interval can be expressed as

$$\begin{split} \mathbf{e}_{\mathbf{r}}(\tau) &= \sqrt{2P_{\mathbf{r}}} \quad \left\{ \left[1 - (\mathbf{M}_{\mathbf{A}^{-}} \ \mathbf{M}_{\mathbf{B}}) \, \mathbf{e}^{-\pi \mathbf{B} \tau} \right] \, \cos \left(\phi_{\mathbf{0}}^{'} \right) \right. \\ &+ \left. \mathbf{M}_{\mathbf{C}} \mathbf{e}^{-\pi \mathbf{B} \tau} \sin \left(\phi_{\mathbf{0}}^{'} \right) \right\} \, \cos \left(\omega_{\mathbf{N}} \tau \right) \\ &- \sqrt{2P_{\mathbf{r}}} \quad \left\{ \left[1 - \left(\left[\frac{\Delta f_{\mathbf{N}}}{f_{\mathbf{c}}} \right] + \mathbf{M}_{\mathbf{A}} + \mathbf{M}_{\mathbf{B}} \right) \mathbf{e}^{-\pi \mathbf{B} \tau} \right] \, \sin \left(\phi_{\mathbf{0}}^{'} \right) \right. \end{split}$$

where the distortion terms M_A, M_B, and M_C, involving various waveform and antenna parameters, are similar to equation 10 developed for the isolated transition.

The phase angle d is expressed in terms

+ $M_C e^{-\pi B \tau} \cos(\phi_0)$ $\sin(\omega_N \tau)$

The phase angle ϕ_0 is expressed in terms of the initial phase angle ϕ_0 as

$$\phi'_{0} = \phi_{0} + \sum_{j=1}^{N-1} \omega_{j}^{T}$$
 (16)

Because ϕ_0 is taken to be a uniformly distributed angle between $-\pi$, π , the angle angle ϕ_0 is a similarly distributed random variable. Proceeding as before and considering the uniformly distributed phase angle ϕ_0 in which case M_B = M_C = 0, the the average received symbol energy is determined to be

$$\frac{E_{S}}{E_{-}'} = 1 - 2M_{A}' \left(\frac{1 - e^{-\pi BT}}{\pi BT} \right)$$
 (17)

where, the distortion factor $M_{A}^{'}$ is given by

$$M_A' = M_A + \frac{\Delta f_N}{2f_C}$$
 (18)

$$=\sum_{i=1}^{N-1} \left[\frac{\Delta f_i}{2f_c} \right] e^{-\pi (N-i)BT}$$
 (19)

Because of the dependence of Δf_i upon the random source data, the factor M_A is itself a discrete random variable.

The problem now is reduced to describing a useful closed form expression

for equation 19 for a modulation waveform of interest. In this regard, the remaining discussion is specialized for binary-FSK modulation.

c. <u>Multiple Frequency Transitions</u> (Binary-FSK)

Specializing the discussion to binary-FSK waveform modulation, equation 19 can be expressed as

$$M_A' = \frac{1 - \Delta f}{2f_c} \sum_{i=1}^{N} D_i e^{-\pi (N-i)BT_b}$$
 (20)

where T = $T_{\rm b}$ is the bit duration and $D_{\rm i}$ = (1,0,-1) is a zero mean, tri-state, discrete random variable. For the purpose of approximating the loss in performance, the received energy-per-bit will be defined as

$$\frac{E_{b}}{E_{b}^{'}} = 1 - \sigma_{S} \tag{21}$$

where σ_S is the standard deviation of the normalized bit energy. By examining the joint statistics of $D_{\hat{1}}D_{\hat{1}}$ and evaluating the standard deviation σ_S , it is found that

$$\frac{\mathcal{E}_{b}}{\mathcal{E}_{b}'} = 1 - \frac{|\Delta f|}{\sqrt{2} f_{c}} \left(\frac{1}{1 + e^{-\pi BT}} \right)^{1/2} \left(\frac{1 - e^{-\pi BT}}{\pi BT} \right)$$

Equation 22 is also plotted in Fig. 3 as a function of BT and several values of $I\Delta fI/f_C$.

The results are truly impressive when one considers that the modulated signal is being passed through an antenna with an instantaneous bandwidth several orders of magnitude less than that of the signal.

IV. Simulation Results

To support the results of the preceding analysis, the synchronously tuned antenna is modeled as a sampled data filter and evaluated using binary FSK and MSK waveform modulations. In deriving the antenna circuit model for the simulation program, advantage is taken of the fact that the antenna looks like a time-invariant network over some finite time interval. The simulation model implements the response described by equation 8. In this context, the state transition matrix projects the output response from one sample to another and the initial conditions

are constantly updated at the sampling instants.

The simulation model is used to simulate the performance of non-coherently detected binary-FSK waveform modulation having unity modulation index, i.e. $\Delta f = R_b$. The degradation at $P_{be} = 10^{-3}$ is about 0.1 dB, which is about 0.1 dB less than that predicted from Fig. 3.

V. <u>Conclusions</u>

The analysis and simulation results demonstrate that synchronous antenna tuning offers significant performance gains over fixed tuned antenna systems. Fig. 4 summerizes the results as a function of the BT product for MSK modulation.

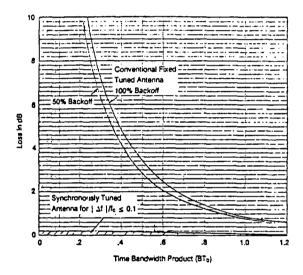


Figure 4. Comparison of Signal Loss for an MSK Modulated Waveform

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